

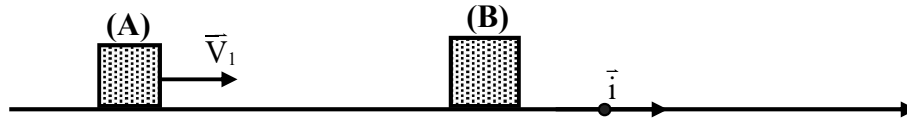
This exam is formed of three exercises in three pages.
The use of non-programmable calculators is recommended.

First exercise: (6 points)**Collision and interaction**

In order to study the collision between two bodies, we consider a horizontal air table equipped with a launcher and two pucks (A) and (B) of respective masses $m_A = 0.4 \text{ kg}$ and $m_B = 0.6 \text{ kg}$.

(A), launched with the velocity $\vec{V}_1 = 0.5 \vec{i}$, collides with (B) initially at rest.

(A) rebounds with the velocity $\vec{V}_2 = -0.1 \vec{i}$ and (B) moves with the velocity $\vec{V}_3 = 0.4 \vec{i}$ (V_1 , V_2 and V_3 are expressed in m/s). Neglect all frictional forces.

**A – Linear momentum**

- 1) a) Determine the linear momentums:
 - i) \vec{P}_1 and \vec{P}_2 of (A), before and after collision respectively;
 - ii) \vec{P}_3 of (B) after collision.
 - b) Deduce the linear momentums \vec{P} and \vec{P}' of the system [(A), (B)] before and after collision respectively.
 - c) Compare \vec{P} and \vec{P}' . Conclude.
- 2) a) Name the external forces acting on the system [(A), (B)].
 - b) Give the value of the resultant of these forces.
 - c) Is this resultant compatible with the conclusion in question (1- c)? Why?

B – Type of collision

- 1) Determine the kinetic energy of the system [(A), (B)] before and after collision.
- 2) Deduce the type of the collision.

C – Principle of interaction

The duration of collision is $\Delta t = 0.04 \text{ s}$; we can consider that $\frac{\Delta \vec{P}}{\Delta t} \approx \frac{d\vec{P}}{dt}$.

- 1) Determine during Δt :
 - a) the variations $\Delta \vec{P}_A$ and $\Delta \vec{P}_B$ in the linear momentums of the pucks (A) and (B) respectively;
 - b) the forces $\vec{F}_{A/B}$ exerted by (A) on (B) and $\vec{F}_{B/A}$ exerted by (B) on (A).
- 2) Deduce that the principle of interaction is verified.

Second exercise: (7 points)**Characteristic of an electric component**

In order to determine the characteristic of an electric component (D), we connect up the circuit represented in figure 1.

This series circuit is composed of: the component (D), a resistor of resistance $R = 100 \Omega$, a coil ($L = 25 \text{ mH}$; $r = 0$) and an (LFG) of adjustable frequency f maintaining across its terminals a sinusoidal alternating voltage $u = u_{AM}$.

A – First experiment

We connect an oscilloscope so as to display the variation, as a function of time, the voltage u_{AM} across the generator on the channel (Y_1) and the voltage u_{BM} across the resistor on the channel (Y_2).

For a certain value of f , we observe the waveforms of figure 2.

The adjustments of the oscilloscope are:

- ✓ vertical sensitivity: 2 V/div on the channel (Y_1);
0.5 V/div on the channel (Y_2);
- ✓ horizontal sensitivity: 1 ms/div.

- 1) Redraw figure 1 and show on it the connections of the oscilloscope.
- 2) Using figure 2, determine:
 - a) the value of f and deduce the value of the angular frequency ω of u_{AM} ;
 - b) the maximum value U_m of the voltage u_{AM} ;
 - c) the maximum value I_m of the current i in the circuit;
 - d) the phase difference φ between u_{AM} and i . Indicate which one leads the other.
- 3) (D) is a capacitor of capacitance C . Justify.
- 4) Given that: $u_{AM} = U_m \sin \omega t$. Write down the expression of i as a function of time.
- 5) Show that the expression of the voltage across the capacitor is:

$$u_{NB} = - \frac{0.02}{250\pi C} \cos \left(\omega t + \frac{\pi}{4} \right) \quad (u_{NB} \text{ in V ; } C \text{ in F ; } t \text{ in s})$$

- 6) Applying the law of addition of voltages and by giving t a particular value, determine the value of C .

B – Second experiment

The effective voltage across the generator is kept constant and we vary the frequency f . We record for each value of f the value of the effective current I .

For a particular value $f = f_0 = \frac{1000}{\pi} \text{ Hz}$, we notice that I admits a maximum value.

- 1) Name the phenomenon that takes place in the circuit for the frequency $f = f_0$.
- 2) Determine again the value of C .

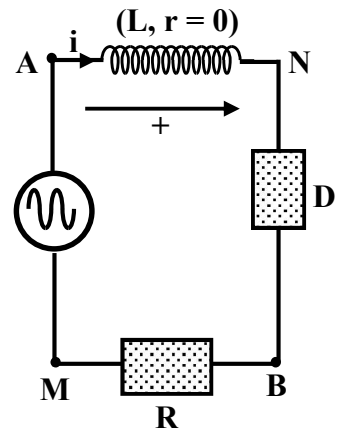


Fig.1

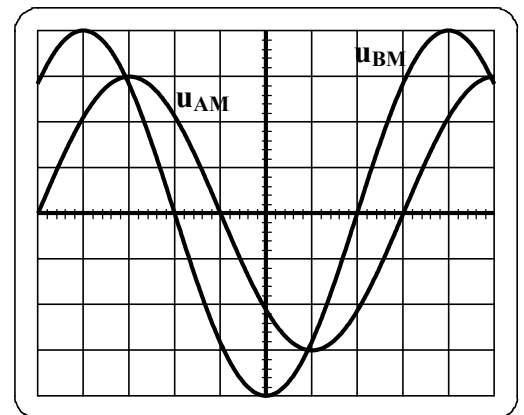


Fig.2

Third exercise: (7 points)**Nuclear reactions**

Given: mass of a proton: $m_p = 1.0073 \text{ u}$; mass of a neutron: $m_n = 1.0087 \text{ u}$;

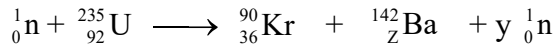
mass of ${}^{235}_{92}\text{U}$ nucleus = 235.0439 u ; mass of ${}^{90}_{36}\text{Kr}$ nucleus = 89.9197 u ;

mass of ${}^{142}_{56}\text{Ba}$ nucleus = 141.9164 u ; molar mass of ${}^{235}_{92}\text{U} = 235 \text{ g/mole}$;

Avogadro's number: $N_A = 6.022 \times 10^{23} \text{ mol}^{-1}$; $1 \text{ u} = 931.5 \text{ MeV}/c^2 = 1.66 \times 10^{-27} \text{ kg}$; $1 \text{ MeV} = 1.6 \times 10^{-13} \text{ J}$.

A – Provoked nuclear reaction

As a result of collision with a thermal neutron, a uranium 235 nucleus undergoes the following reaction:



- 1) a) Determine y and z .
b) Indicate the type of this provoked nuclear reaction.
- 2) Calculate, in MeV, the energy liberated by this reaction.
- 3) In fact, 7% of this energy appears as a kinetic energy of all the produced neutrons.
 - a) Determine the speed of each neutron knowing that they have equal kinetic energy.
 - b) A thermal neutron, that can provoke nuclear fission, must have a speed of few km/s; indicate then the role of the “moderator” in a nuclear reactor.
- 4) In a nuclear reactor with uranium 235, the average energy liberated by the fission of one nucleus is 170 MeV.
 - a) Determine, in joules, the average energy liberated by the fission of one kg of uranium ${}^{235}_{92}\text{U}$.
 - b) The nuclear power of such reactor is 100 MW. Calculate the time Δt needed so that the reactor consumes one kg of uranium ${}^{235}_{92}\text{U}$.

B – Spontaneous nuclear reaction

- 1) The nucleus krypton ${}^{90}_{36}\text{Kr}$ obtained is radioactive. It disintegrates into zirconium ${}^{90}_{40}\text{Zr}$, by a series of β^- disintegrations.
 - a) Determine the number of β^- disintegrations.
 - b) Specify, without calculation, which one of the two nuclides ${}^{90}_{36}\text{Kr}$ and ${}^{90}_{40}\text{Zr}$ is more stable.
- 2) Uranium ${}^{235}_{92}\text{U}$ is an α emitter.
 - a) Write down the equation of disintegration of uranium ${}^{235}_{92}\text{U}$ and identify the nucleus produced.

Given:

Actinium ${}_{89}\text{Ac}$	Thorium ${}_{90}\text{Th}$	Protactinium ${}_{91}\text{Pa}$
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- b) The remaining number of nuclei of ${}^{235}_{92}\text{U}$ as a function of time is given by: $N = N_0 e^{-\lambda t}$ where N_0 is the number of the nuclei of ${}^{235}_{92}\text{U}$ at $t_0 = 0$ and λ is the decay constant of ${}^{235}_{92}\text{U}$.
 - i) Define the activity A of a radioactive sample.
 - ii) Write the expression of A in terms of λ , N_0 and time t .
- c) Derive the expression of $\ln(A)$ in terms of the initial activity A_0 , λ and t .
- d) The adjacent figure represents the variation of $\ln(A)$ of a sample of ${}^{235}_{92}\text{U}$ as a function of time.
 - i) Show that the shape of the graph, in the adjacent figure, agrees with the expression of $\ln(A)$.
 - ii) Using the adjacent figure determine, in s^{-1} , the value of the radioactive constant λ .
 - iii) Deduce the value of the radioactive period T of ${}^{235}_{92}\text{U}$.

